First Takeoff of a Flying Microrobot With No Moving Parts

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Abstract—The preponderance of research into flying micro-
robots has focused on biomimetic flight mechanisms. In this
work, we demonstrate an insect-scale robot capable of vertical
takeoff using electrohydrodynamic thrust, a mechanism with
no natural analogue. The 10mg, 1.8cm by 1.8cm “ionocraft”
operates at about 2400 volts and has a thrust to weight ratio of
approximately 10. Feasibility of using individually addressable
thrusters in a quadcopter-esque manner for attitude control is
demonstrated qualitatively. A combination of design choices in
the microfabricated silicon electrodes and a machine-fabricated
external fixture allow for reproducible hand-assembly of the
microrobot.

I. INTRODUCTION

While autonomous or semi-autonomous flying robots (drones) are already poised to disrupt a multitude of industries including logistics and photography, we have only just begun to explore the possible uses for this technology. Flying micro-
robots open up a new application space where unobtrusiveness and fine data granularity are keys to success. It is possible
to imagine a future where microrobots serve as the spiritual
successor to the wireless sensor, acting as self-installing net-
works or self-directed diagnostic tools. The ability to batch
fabricate microrobots at a low unit cost will enable us to use
them as disposable, versatile swarms [1]. Current work toward
this end largely involves pico air vehicles, defined as having
a maximum takeoff mass of 500 mg or less and maximum
dimensions of 5 cm or less, which have a unique set of scale-
dependent challenges [2]. To date, research has largely focused
on biologically inspired mechanisms, specifically flying insects
like the bee, for inspiration [3] [4].

Biomimetic designs may succeed in replicating the agility
of a flying insect, but the evolution of the flapping wing
mechanism did not happen in the absence of other biological
factors. In the resource constrained field of microrobotics,
it is possible that mimicking the flight of an insect may
necessitate a specific design space. For that reason, we believe
that developing new flight mechanisms for flying microrobots
may lead to otherwise impossible applications, platforms, and
discoveries. The thrust for our flying robot will be generated
electrohydrodynamically (EHD); that is, by using the flow of
ions to generate a momentum transfer in the opposite direction
of desired flight. The flow of neutral air through the collector
electrode due to collisions with the moving ions represents
the net momentum transfer of the system, analogous to how a
propeller accelerates some mass of air to produce thrust. EHD
thrusters are silent, have a high thrust to weight ratio due to
requiring only sparse electrodes to produce useful work, and
are mechanically robust due to their lack of moving parts.

The “ion wind” effect was studied as early as 1700 and
explored by minds such as Newton, Faraday, and Maxwell [5].
Modern understanding of the effect was formalized in seminal
papers by Christenson, Moller, and Robison [6] [7]. While
these provided explanations and derivations of the governing
physical models, little was done in the application space
until decades later. In the 1960s the effect was studied for
use in aircraft, even being featured on the cover of Popular
Mechanics in 1964, but the conclusion was that EHD thrust
was ill-suited for these goals. Today the most widely known
use of EHD thrust may be with the “lifter” model popular with
students and hobbyists. The lifter is on the order of one square
meter, typically constructed from balsa wood and aluminum
foil, and can provide sufficient lift for take off when connected
to a high voltage (30kV) power supply.

A. Electrohydrodynamic Force

It is possible to derive an expression for EHD thrust in terms
of ion current starting from the Coulomb force acting on a
volume of ions occupying a gap [8]. This one dimensional
model assumes that electrode cross sectional area is large
compared to the gap length, $d$. 

![Fig. 1. These “quad-thrusters” are made of microfabricated silicon electrodes and fused silica capillary tubes and assembled by hand. They are 1.8cm x 1.8cm, 10mg, with four individually addressable electrode sets, and a 1mm electrode gap. They should be capable of producing around 1mN of force for a thrust to weight ratio of about 10.](image_url)
\[ F = \int \rho E dV = \int \rho E Adx = \int \frac{Id V}{\mu VA} dAdx = \frac{Id}{\mu} \] (1)

Where \( I \) is ion current and \( \mu \) is the ion mobility. A more useful two-dimensional model can also be derived from the Coulomb electric force and some fundamental definitions.

\[ Q_0 = CV_{drive} = \epsilon_0 LV_{drive} \] (2)

\[ Q_{gap} = \alpha Q_0 \] (3)

In the preceding equations we have assumed that the ions (charges) are injected into a cubic capacitive gap by some mechanism. This then yields the \( \alpha \) coefficient which has a maximum value of 9/8, as dictated by the Mott-Gurney law (4) which states that there is a space charge saturation limit of the conduction current density.

\[ J = \frac{(9/8) \epsilon \mu V^2}{L^3} \] (4)

Finally, electrostatic force on the ions injected into the gap is given in Eqn. 5. Note that this is force acting on the ions; direct translation of this to thrust requires that all momentum is transferred in the preferred thrust direction by ion-neutral collisions.

\[ F = Q_{gap}E_{drive} = \alpha \epsilon_0 LV_{drive}E_{drive} = \alpha \epsilon_0 L^2 E_{drive}^2 \] (5)

With thrust efficiency in terms of Newtons per Watt of:

\[ I = \frac{QV}{d} = \alpha \epsilon_0 \frac{A}{d^3} \mu V^2 \] (6)

\[ P = IV = \alpha \epsilon_0 \frac{A}{d^3} \mu V^3 \] (7)

\[ \frac{F}{P} = \frac{d}{\mu V} = \frac{1}{\mu E} \] (8)

The electrical efficiency equation (8) shows that, at the breakdown field in air of \( 3 \times 10^4 \text{V/m} \) and using an ion mobility in air of \( 2 \times 10^{-4} \text{m}^2/\text{V s} \), the efficiency will be approximately \( 2 \times 10^N \). Assuming a constant ion mobility and that all momentum is transferred in the preferred direction, this efficiency is a theoretical minimum for ion thrust.

To illustrate this design space we can plot the EHD theoretical thrust versus efficiency curve (in Newtons per Watt), shown in Fig. 3. This plot is not meant to be a conclusive comparison between flying microrobots; it serves to show that EHD has the potential to provide high thrust compared to biomimetic designs at the cost of efficiency. Conversely, simply lowering the applied DC voltage and hence decreasing the ion drift field can increase the efficiency while decreasing the thrust to levels similar to that achieved by flapping wing microrobots. It should be noted that at identical efficiency levels, there will theoretically be less thrust than from a flapping wing mechanism. We stipulate that the various other benefits of EHD thrust, e.g. silent flight and high thrust to weight ratio, still make it an attractive alternative.

B. Corona Discharge

An electrohydrodynamic thruster requires both a way to accelerate ions to produce force as well as a way to generate them. A common method for producing the ions is corona discharge, which has been adopted for commercial applications including electrostatic precipitators and mass spectrometers. Corona discharge as a mechanism to produce an ion drift current has been separately studied at electrode gaps down to hundreds of micrometers [10].

Corona discharge is an atmospheric-pressure ionization process characterized by a self-sustained plasma localized around a charged conductor, the emitter, and ionic current flowing to a second electrode, the collector. The corona region is generated primarily by strong electric fields arising due to geometric effects, e.g. a small diameter wire or sharp point [11]. The magnitude of the discharge is typically space-charge
limited, with the polarity determined by whether high voltage is applied to the emitter (“positive corona discharge”) or the collector (“negative corona discharge”).

The critical field criterion for corona discharge inception has been widely used and experimentally verified since the 1920s [12]. Using it, a corona onset potential \( V_0 \) can be defined for a given geometry. For a wire-to-plane geometry, the corona inception voltage is given by:

\[
V_0 = g_0 r_0 \left( 1 + \frac{0.301}{\sqrt{r_0}} \right) \ln \left( \frac{2d}{r_0} \right) \tag{9}
\]

Where \( g_0 \) is the breakdown field strength equal to about 30kV/cm for air, \( r_0 \) is the radius of the emission wire in centimeters, and \( d \) is the distance between the wire and the plane in cm. This equation has been simplified to assume standard temperature and pressure as well as an ideal smooth wire. The ability to microfabricate electrodes with small radii of curvature and to lithographically define small electrode gaps allows for favorable scaling of the corona discharge initiation point.

II. RELATED WORK

Electrohydrodynamic thrust has been revisited as a flight mechanism in recent research. Masuyama et al. verified the theoretical framework of EHD thrust and concluded through extensive experimentation that thrust-to-power ratios are comparable with many conventional propulsion mechanisms [13]. Further work concluded that due to the experimentally measured thrust densities on the order of 10Nm\(^{-3}\), EHD propulsion is most suited for small UAV applications [14]. It should be noted that thrust densities measured in this work are two orders of magnitude higher than this value.

A large amount of work has been performed simulating and optimizing corona discharge-based EHD systems. The typical approach combines the critical field criterion established by Peek with the Kaptzov hypothesis, which stipulates that the electric field on the corona emitter surface remains constant at Peek’s critical value even as applied voltage increases. Surface charge density and subsequently the space charge region can then be solved for, yielding a numerical solution for ion current due to drift. Typical simulation performed in this manner agrees to within about 10% with experimental values [15]. Combining this approach with a diffuse species collision model and a flow model yields a simulated measure of air flow; this approach has also been verified experimentally [16].

Miniaturized EHD devices have been used as low power convection coolers and for ion spectrometry tools. A microfabricated EHD cooling device has been demonstrated with an operating voltage around 1000V [17]. Corona discharge in air has been found to be a relatively stable, repeatable, and high current ionization source for ion mobility spectrometry [18]. Microfabricated corona discharge based devices have shown promise as portable airborne particle analyzers and separators [19].

Fig. 5. The simple two mask silicon-on-insulator (SOI) process to fabricate the silicon electrodes. First the 40 \( \mu \)m device silicon is patterned. The wafer is flipped and loosely bonded to a handle wafer using a thermally conductive grease. The 500 \( \mu \)m handle silicon is aligned, patterned, and then etched to plasma dice the individual devices. Finally, tweezers are used to physically remove the electrodes, breaking the buried oxide in the process. The electrodes are placed into a vapor HF etcher to clear the remaining oxide.

III. FABRICATION AND ASSEMBLY

Electrode geometries were chosen based on a combination of lessons learned from previous efforts to create meso-scale EHD thrusters (e.g., limits of repeatable gap scaling for a given emitter radius), availability of a stable fabrication process with the given wafer properties, and feasibility of hand assembly (e.g., minimum size to handle with tweezers). Devices are fabricated in a two mask silicon-on-insulator (SOI) process and individually plasma diced. The active electrode material is all device-side silicon, allowing for a high thrust to weight ratio as the force is a predominantly two dimensional effect. The process flow is depicted in Fig. 5. After the backside deep
reactive ion etch, the devices are physically removed from the wafer with tweezers and etched with vapor HF to clear the buried oxide layer. Corona discharge is a strong function of electrode geometry; care must be taken in designing the electrodes to prevent early breakdown, reverse corona (where a plasma is formed around the collector), and wasted area. Exterior corners are filleted and only rounded shapes are used in non-functional area, e.g. near the dielectric standoff attachment points.

Fused silica capillary tubing with an inner radius of about 400 $\mu$m and a wall thickness of 25 $\mu$m is used for the dielectric posts that set the distance between the two electrodes. The device is designed so that they can be fabricated in a stack - a rendered depiction of the device assembly is shown in Fig. 7. An aluminum jig is used during the assembly process to assist with placement and alignment of the silica tubes. An assembled ionocraft is about 10mg and 1.8cm by 1.8cm (see Fig. 1). It takes roughly thirty minutes to assemble by hand.

Using 60 $\mu$m diameter copper wires as the power connections the device was actuated in front of a high speed camera. At about 2400V the ionocraft took flight, reaching a peak attitude of around 5cm before the instability of its attitude caused a power wire to touch the collector grid. This flight is shown in Fig. 4. From this video a peak acceleration of about 2 gravities can be calculated, corresponding to a force of about 200 $\mu N$, far below the theoretical maximum force these devices should be able provide. During the video the voltage was being slowly increased by hand and, due to the high thrust to weight ratio, the device took off and subsequently crashed before the voltage could be increased to the levels used to measure the maximum thrust point.

The goal of using four individually addressable electrode sets is to allow for attitude control similar to that of a quadcopter. As an initial feasibility test, only two of the four thrusters were actuated. As shown in Fig. 6, this created a moment around the center axis and the ionocraft flipped over as predicted. The question of how to control yaw remains open. A traditional quadcopter controls yaw by coupling torque from its rotors to produce a net moment around only one axis; the EHD thruster presented here has no analogaus torque component. One possibility is to angle the emitter electrode along the vertical axis in order to produce horizontal force,
although this would lead to decreased vertical force.

V. CONCLUSIONS AND NEXT STEPS

While takeoff and the feasibility of attitude control has been demonstrated, the path to an autonomous ioncraft requires advancement on a number of fronts. Light weight and low power sensing, computation, control, and communications modules all need to be integrated; although the ioncraft has a high thrust to weight ratio, it is still a relatively low amount of force and we expect the microrobot to have a highly constrained mass budget. To save on payload mass, it may be possible to use an ion thruster as both a sensor and an actuator; changes in ion mobility and hence output force can be related to humidity or pressure. The electrostatic precipitation effect can clean the air while providing thrust for the robot to fly [20].

A controller needs to be implemented that takes into account the EHD thrust nonlinearities; beyond requiring further characterization of the thrust mechanism itself, it will also require development of low mass and high speed high-voltage switching circuitry. Previous work has demonstrated SOI CMOS circuits with NMOS breakdown voltages above 50V and PMOS close to 100V, which could be increased further with process optimization or worked around in circuit design [21]. Because body dynamics increase in speed with decreased size, it may be necessary to implement some form of passive stability into the mechanical design to decrease the required controller bandwidth [22].

Finally, everything needs to be powered by a high energy density, high-voltage battery array. Thin, high aerial density printable lithium ion batteries have been demonstrated that could potentially power an ioncraft given further thickness reduction to increase discharge rate [23]. The operating voltage must be decreased to minimize series resistance losses and potential breakdown events in the power array; this will require further optimization of the electrode sets and likely changing the assembly process to allow for lithographically defined electrode gaps.

It is possible to imagine using the microfabricated atmospheric ion thruster presented here as a component in other microrobotic platforms. Previous research has demonstrated lift to drag ratios in excess of 10 from centimeter-scale wings [24]; ion thrusters could be used like jets under similar wings to increase their effective lift [25]. Their planar geometry and high thrust to weight ratio means it is also possible they could be incorporated onto walking platforms for short range “hops” over unfavorable terrain.

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REFERENCES